GCSE Mathematics Topics

1. Number

- Basic Arithmetic: Addition, subtraction, multiplication, division.
- Order of Operations: BIDMAS/BODMAS (Brackets, Indices, Division/Multiplication, Addition/Subtraction).

• Fractions, Decimals, and Percentages:

- o Converting between them.
- Calculating percentages of amounts.
- o Percentage increase/decrease.

Factors, Multiples, and Primes:

- o Prime factorization.
- Highest Common Factor (HCF).
- Lowest Common Multiple (LCM).

• Standard Form:

- o Writing numbers in standard form.
- o Calculating with standard form.

Surds:

- Simplifying surds.
- Rationalizing the denominator.

• Estimation:

- o Rounding numbers to significant figures or decimal places.
- Using approximations in calculations.

• Recurring Decimals:

Converting recurring decimals to fractions.

2. Algebra

• Basic Algebraic Manipulation:

- o Simplifying expressions.
- Expanding and factoring.

• Equations and Inequalities:

- Solving linear equations.
- Solving quadratic equations (factoring, completing the square, quadratic formula).
- Solving simultaneous equations (linear/linear or linear/quadratic).
- Solving inequalities and representing them on number lines.

Graphs and Coordinates:

- o Plotting linear, quadratic, and cubic graphs.
- o Understanding gradients and intercepts of linear graphs.
- o Identifying roots, turning points, and symmetry of quadratic graphs.

• Sequences:

- Finding nth terms of linear and quadratic sequences.
- o Arithmetic and geometric sequences.

Functions:

o Basic function notation (e.g., f(x)f(x)f(x)).

Composite functions.

3. Ratio, Proportion, and Rates of Change

Ratios and Proportions:

- Simplifying ratios.
- Sharing amounts in a given ratio.
- o Direct and inverse proportion.

• Speed, Distance, and Time:

Using formulas for speed and rates of change.

• Scale Factors:

- Enlargement of shapes using scale factors.
- Maps and scales.

• Gradients and Rates:

Understanding gradients as rates of change.

4. Geometry and Measures

• Basic Geometry:

- o Angles in polygons.
- o Parallel and perpendicular lines.
- o Properties of triangles and quadrilaterals.

• Transformations:

o Translations, rotations, reflections, and enlargements.

• Circle Theorems:

- o Angles in a circle.
- Tangents and chords.

• Pythagoras' Theorem:

- Applying to right-angled triangles.
- Using in 3D problems.

Trigonometry:

- o Sine, cosine, and tangent ratios.
- Calculating angles and sides in right-angled triangles.
- o Solving problems in 2D and 3D.

• Mensuration:

- Area and perimeter of 2D shapes.
- Surface area and volume of 3D solids (e.g., spheres, cylinders, cones, pyramids).

Vectors:

- Adding and subtracting vectors.
- Representing vectors graphically and algebraically.

• Constructions and Loci:

o Constructing bisectors and loci using a compass and ruler.

5. Probability

• Basic Probability:

- o Probability scales (0 to 1).
- o Single-event probability.

Combined Events:

- o Tree diagrams.
- o Independent and dependent events.
- Mutually exclusive events.

• Expected Outcomes:

• Using probabilities to predict outcomes over multiple trials.

6. Statistics

• Data Collection:

- o Primary and secondary data.
- o Sampling methods (random, stratified).

• Data Representation:

- o Bar charts, pie charts, and histograms.
- o Scatter graphs (correlation).
- o Cumulative frequency graphs.

Measures of Central Tendency:

- o Mean, median, mode.
- Range and interquartile range (IQR).

• Probability Distributions:

• Understanding distributions and trends.